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# Sirindhorn International Institute of Technology Thammasat University at Rangsit 

School of Information, Computer and Communication Technology

## ECS 203: Problem Set and Tutorial 12

Semester/Year: 2/2015
Course Title: Basic Electrical Engineering
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Course Web Site: http://www2.siit.tu.ac.th/prapun/ecs203/

## Due date: Not Due

## Instructions

1. All phasor should be answered in polar form where the magnitude is positive and the phase is between $-180^{\circ}$ and $180^{\circ}$.
2. All sinusoid should be answered in the cosine form where the amplitude is positive and the phase is between $-180^{\circ}$ and $180^{\circ}$.

## Questions

1) [Alexander and Sadiku, 2009, Q9.17] Two voltages $v_{1}$ and $v_{2}$ appear in series so that their sum is $v=v_{1}+v_{2}$.
If $\mathrm{v}_{1}=10 \cos (50 t-\pi / 3) \mathrm{V}$ and $\mathrm{v}_{2}=12 \cos \left(50 t+30^{\circ}\right) \mathrm{V}$,
Simplify v. (Your answer should be a time-dependent sinusoid in standard form.)
$\qquad$ ID: $\qquad$
2) [Alexander and Sadiku, 2009, Q9.56] At $\omega=377 \mathrm{rad} / \mathrm{s}$, find the input impedance of the circuit shown in Figure 1.


Figure 1
Remark: Impedance value should be answered in rectangular form. Unit is $\Omega$.
3) [F2010] In this question, you must use the specified techniques to solve the problem. There will be no credit given if you do not follow the instructions. As always, your score depends strongly on your explanation of your answer. If the explanation is incomplete, zero score may be given even when the final answer is correct.

Consider the circuit below.


Figure 2
Suppose

$$
\begin{gathered}
v_{s}(t)=7 \cos \left(200 t+30^{\circ}\right) \mathrm{V}, \\
\mathrm{R}_{1}=6 \Omega, \mathrm{R}_{2}=4 \Omega, \text { and } L=5 \mathrm{mH} .
\end{gathered}
$$

a. Find $\mathbf{V}_{s}$ (which is the phasor representation of $\mathrm{v}_{\mathrm{s}}(\mathrm{t})$ ).
b. Find the impedance of the inductor. ID: $\qquad$
c. Use nodal analysis to find the voltage $v_{2}(t)$ across the resistor $\mathrm{R}_{2}$.
d. Find the voltage $v_{1}(t)$ across the resistor $\mathrm{R}_{1}$.
e. Use mesh analysis to find all mesh currents (in the clockwise direction) in phasor form.
$\qquad$ ID: $\qquad$
f. Use the mesh current(s) to find the current $i_{L}(t)$ through the inductor.
g. Use source transformation(s) and/or impedance combination(s) to transform the part of the circuit to the left of the inductor into a phasor voltage source $\mathbf{V}_{\mathbf{A}}$ in series with an impedance $\mathbf{Z}_{\mathbf{A}}$.
h. Use $\mathbf{V}_{\mathbf{A}}, \mathbf{Z}_{\mathbf{A}}$, and the impedance of the inductor to find $i_{L}(t)$.
$\qquad$ ID: $\qquad$
4) [Alexander and Sadiku, 2009, Q10.43] Using the superposition principle, find $i_{x}$ in the circuit of Figure 3.


Figure 3
5) [Alexander and Sadiku, 2009, Q10.58] For the circuit depicted in Figure 4, find the Thevenin equivalent circuit at terminals $a-b$.


Figure 4
$\qquad$ ID: $\qquad$
6) [Alexander and Sadiku, 2009, Q10.49] Using source transformation, find $i$ in the circuit of Figure 5.


Figure 5
7) [Alexander and Sadiku, 2009, Q11.5] Assuming that $v_{s}(t)=16 \cos \left(2 t-40^{\circ}\right) \mathrm{V}$ in the circuit shown in Figure 6, find the average power delivered to each of the passive elements.


Figure 6
$\qquad$ ID: $\qquad$
8) [F2010] Continue from Question 3. Consider the circuit below.


Figure 7
Suppose

$$
\begin{gathered}
v_{s}(t)=7 \cos \left(200 t+30^{\circ}\right) \mathrm{V}, \\
\mathrm{R}_{1}=6 \Omega, \mathrm{R}_{2}=4 \Omega, \text { and } L=5 \mathrm{mH} .
\end{gathered}
$$

a. Find the instantaneous power absorbed by $R_{1}$.
b. Find the average power absorbed by $\mathrm{R}_{1}$
c. Find the average power absorbed by $L$
d. Find the average power absorbed by the voltage source.

